

## Experimental Results and Modeling

### NaV<sub>2</sub>O<sub>5</sub> Crystals Magnetic Susceptibility

#### Modeling

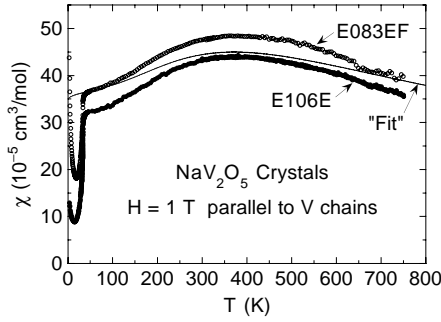
The observed susceptibility  $\chi(T)$  is modeled using

$$\chi(T) = \chi_o + C_{\text{imp}}/(T - \theta_{\text{imp}}) + \chi^{\text{spin}}(T)$$

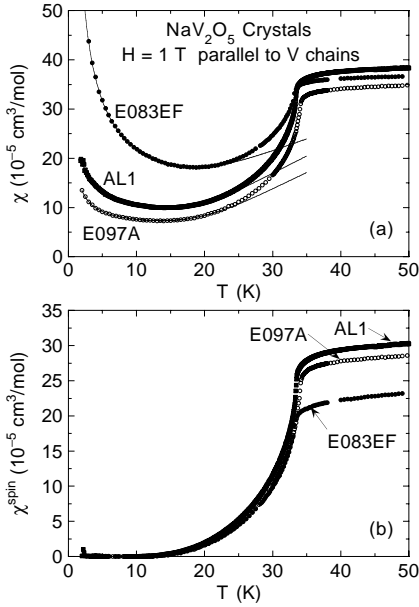
$\chi_o$  is the T-independent term

2nd term: Curie-Weiss impurity/defect term

3rd term: Theoretical spin susceptibility

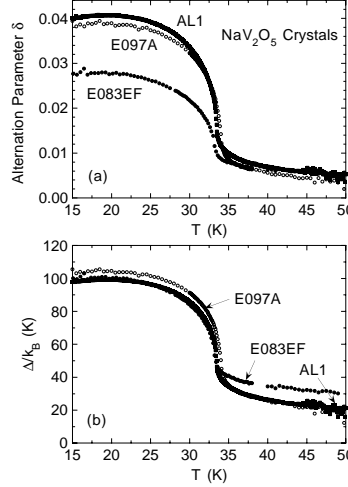


- The  $\chi(T)$  of NaV<sub>2</sub>O<sub>5</sub> crystals (symbols) above  $T_c = 34$  K does not follow the prediction (solid curve "Fit") for the  $S = 1/2$  AF uniform Heisenberg chain, contrary to claims in the literature
- In our modeling below, we assume that this is due to a temperature-dependent exchange constant above  $T_c$



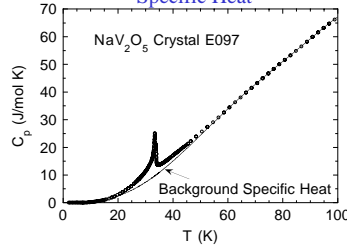
The  $\chi(T)$  of three NaV<sub>2</sub>O<sub>5</sub> crystals at low T is shown in (a). A spin gap develops below  $T_c = 34$  K. The intrinsic spin susceptibility  $\chi^{\text{spin}}(T)$  is obtained by subtracting the  $\chi_o$  and Curie-Weiss impurity and/or defect contributions, as shown in (b)

The spin dimerization  $\delta$  and spin gap  $\Delta$  were extracted from  $\chi^{\text{spin}}(T)$  using our theory:

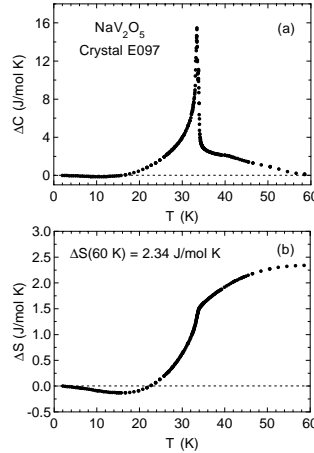


- The  $\Delta(T = 0) = 100$  K in (b) agrees with inelastic neutron scattering results. This is the first determination of  $\Delta(T)$  directly from  $\chi(T)$  data for any alternating-exchange chain
- A spin pseudogap of about 40 K is seen just above  $T_c$ , which decreases with increasing T. This is the first observation of spin dimerization order parameter fluctuations above  $T_c$  in NaV<sub>2</sub>O<sub>5</sub>

#### Specific Heat

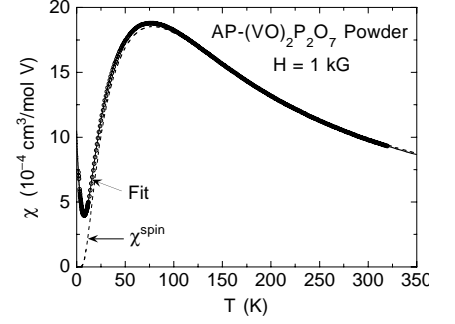


Changes in the specific heat  $\Delta C$  and entropy  $\Delta S$  due to the transition and associated order parameter fluctuations:



- The influence of spin, charge, and/or lattice order parameter fluctuations is seen in the lambda shape of the specific heat anomaly and  $\Delta C$  from  $T_c$  up to at least 60 K
- At  $T_c$ , at least 77% of  $\Delta S$  arises from lattice/charge degrees of freedom and less than 23% from spin degrees of freedom.
- Charge ordering and/or the lattice distortion strongly contribute to the thermodynamics of the transition

### $\chi(T)$ of (VO)<sub>2</sub>P<sub>2</sub>O<sub>7</sub>

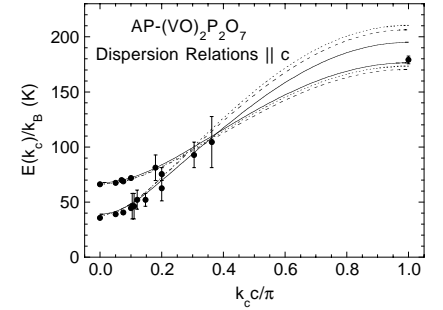


Fit parameters for two distinct AF alternating-exchange chains:

Chain 1:  $J_1 = 130.3(7)$  K,  $J_2 = 109.5(9)$  K,  $\Delta = 38.6(5)$  K  
Chain 2:  $J_1 = 128.8(5)$  K,  $J_2 = 82.6(6)$  K,  $\Delta = 67.5(5)$  K

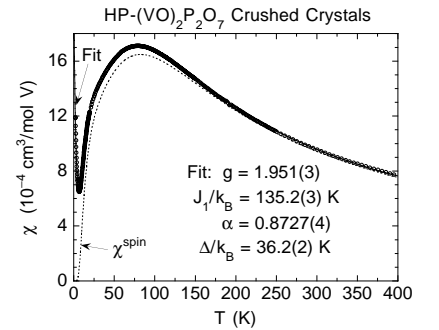
- The two-chain modeling would not have been possible without our high-precision theoretical work on the magnetic susceptibility of alternating-exchange chains
- The two-chain model is consistent with the  $\chi(T)$  data
- The two spin gaps  $\Delta$  are in agreement with neutron scattering data (see below)

One-magnon dispersion relations predicted for the two chains using the above exchange constants:



Neutron scattering data at 10 K (filled circles):  
A.W. Garrett et al., PRL 79, 745 (1997)

- The agreement of our predictions (curves) with the data is good. Our prediction of two absorption peaks at  $k = \pi/c$  is in agreement with more recent neutron data (M. Enderle et al., unpublished)



- The fit in the figure is for a single type of alternating-exchange chain as demanded by the crystal symmetry
- A two-chain fit yielded the same parameters for each of the two chains as shown in the figure. This confirms the validity of our two-chain fit for AP-(VO)<sub>2</sub>P<sub>2</sub>O<sub>7</sub>